

Investigation into the rotational dynamics of the defunct satellite TOPEX/Poseidon



LUC SAGNIÈRES, INNA SHARF, AND
FLORENT DELEFLIE

IWLR2018

CANBERRA, AUSTRALIA
9 NOVEMBER 2018



McGill

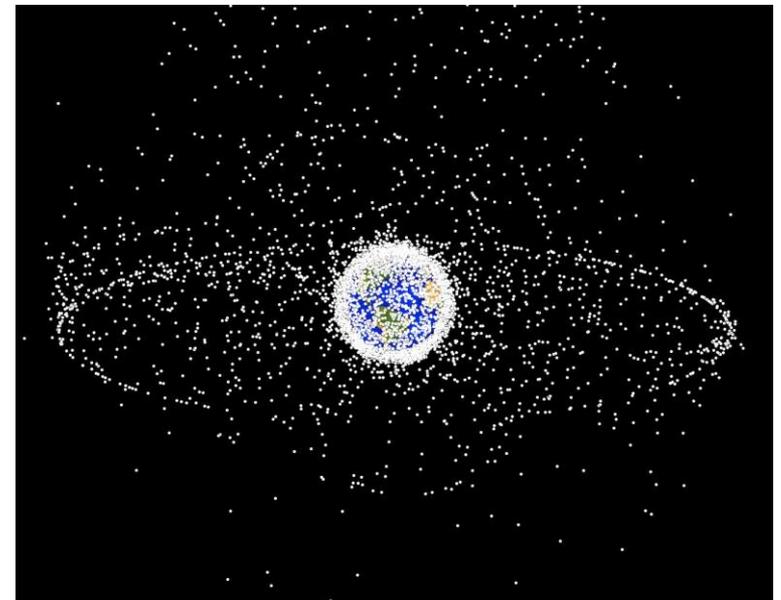


Outline

1) SPACE DEBRIS ATTITUDE DYNAMICS

2) DEBRIS SPIN/ORBIT SIMULATION ENVIRONMENT (D-SPOSE)

3) TOPEX/POSEIDON ATTITUDE ANALYSIS

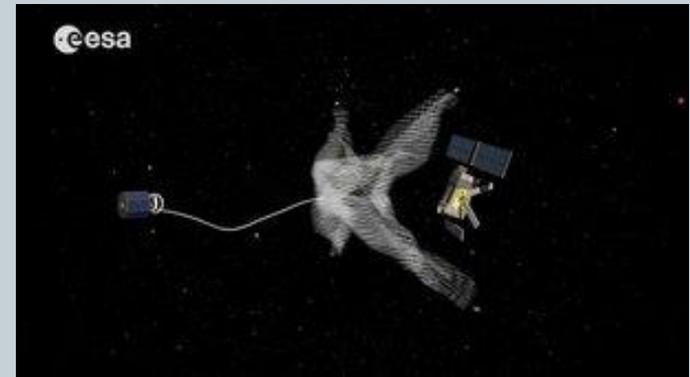


Active Debris Removal (ADR)



- Attempts to de-orbit critical targets being developed.
 - Launch removal spacecraft
 - Rendez-vous with target debris
 - Analyse target motion
 - Stabilize and capture
 - De-orbit and burn

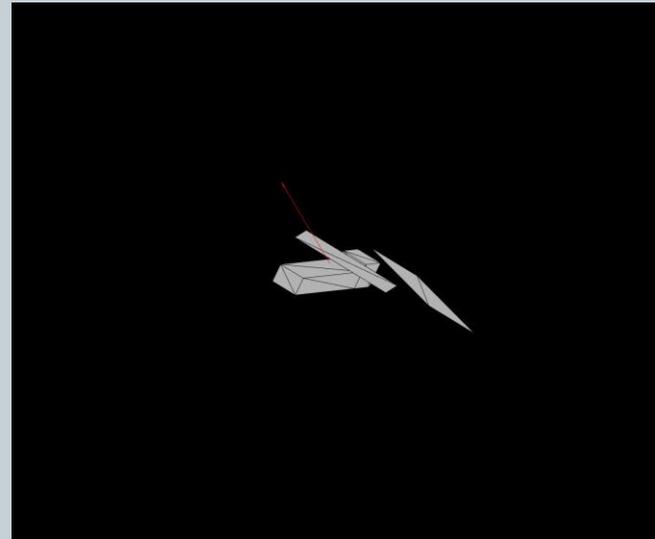
- Capture technologies include:
 - Robotic arm
 - Net
 - Harpoon



Rotational Motion of Space Debris



- Need to accurately know rotational motion of target debris for Active Debris Removal before launch of removal spacecraft
- Environmental torques:
 - Gravity gradient
 - Magnetic torques
 - Aerodynamic torque
 - Radiation torques
 - Particle bombardment
- Accurate attitude estimates also improve orbit predictions for conjunction analyses



Debris Spin/Orbit Simulation Environment (D-SPOSE)



- Can we build a flexible and comprehensive tool to analyze and predict the rotational motion of large space debris?
- Tool will be publicly available by the end of 2018 / early 2019

Model Equations and Perturbations



Orbit:

$$1) \quad \ddot{\mathbf{r}}(t) = -\frac{\mu}{r(t)^3} \mathbf{r}(t) + \sum_j \mathbf{a}_j(t, \mathbf{r}(t))$$

Attitude:

$$2) \quad \mathbf{I}\dot{\boldsymbol{\omega}}(t) + \boldsymbol{\omega}(t)^\times \mathbf{I}\boldsymbol{\omega}(t) = \sum_j \boldsymbol{\tau}_j(t, \mathbf{r}(t))$$

$$3) \quad \dot{\mathbf{q}}(t) = \frac{1}{2} \boldsymbol{\Omega}(\boldsymbol{\omega}) \mathbf{q}(t)$$

| Perturbation | Environmental Model |
|---|---------------------------------------|
| Gravitational perturbations and gravity gradient torque | EGM2008 |
| Third-body perturbations | Ephemeris |
| Aerodynamic drag and torque | DTM-2013; NRLMSISE-00; JB-2008; HWM14 |
| Eddy-current torque | IGRF-12; WMM |
| Solar radiation pressure and torque | Montenbruck and Gill |
| Albedo and IR acceleration and torque | Stephens; CERES; ECMWF |
| Internal energy dissipation | Kane Damper |
| Hypervelocity impacts | Sagnières and Sharf; MASTER-2009 |

Model Input

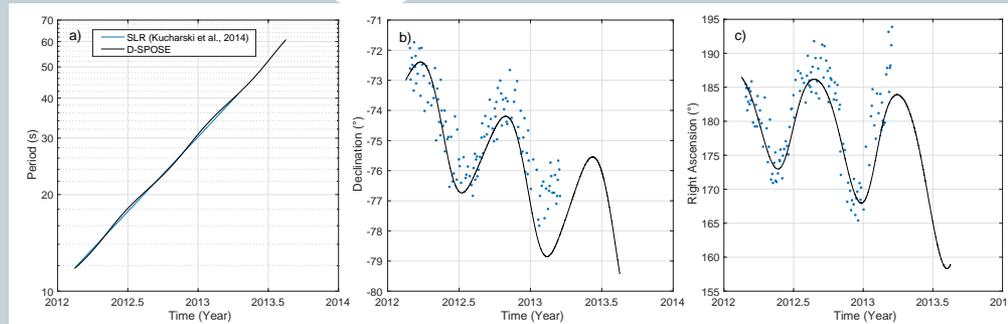


- **Spacecraft Geometry** (list of triangular surfaces)
- **Time Parameters** (propagation length and time step)
- **Spacecraft Parameters** (inertia and magnetic tensors, surface optical coefficients)
- **Initial Conditions** (initial orbit, attitude and angular velocity)
- **Model Parameters** (selected perturbations, chosen environmental models)

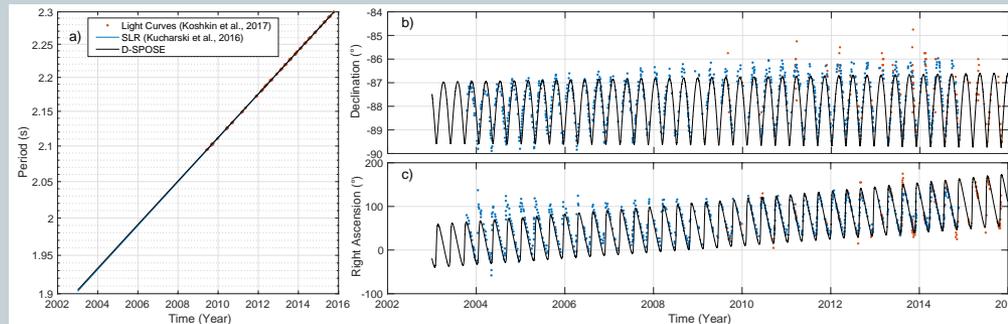
Validation from SLR Observations and Light Curves



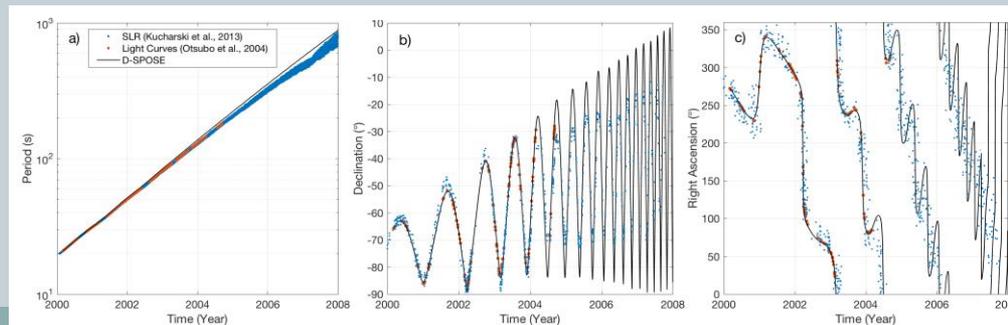
LARES



AJISAI



LAGEOS-2



TOPEX/Poseidon Attitude Analysis

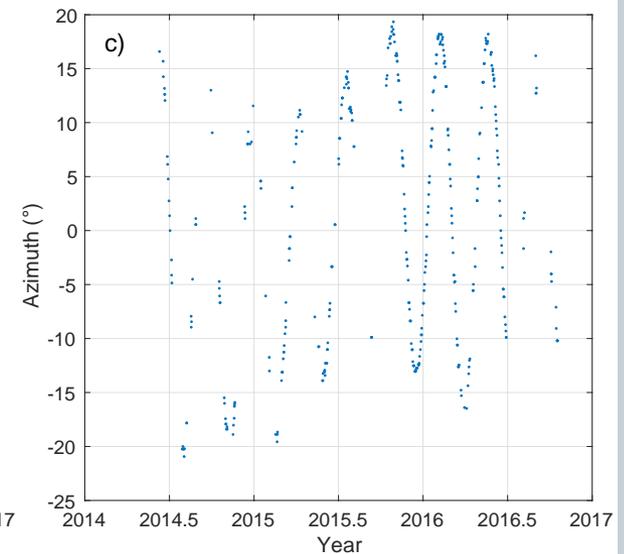
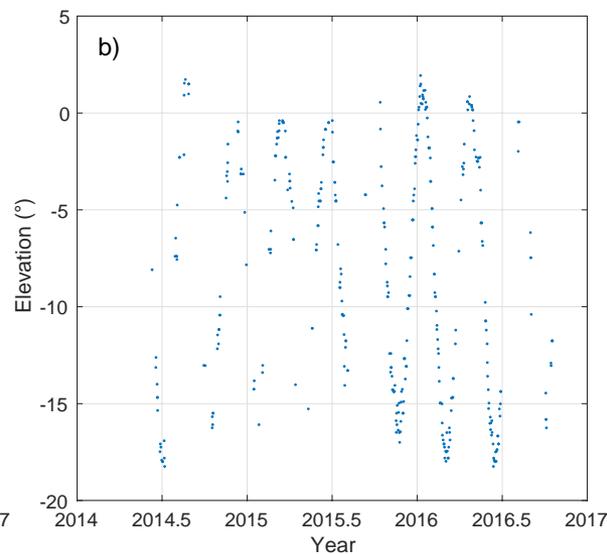
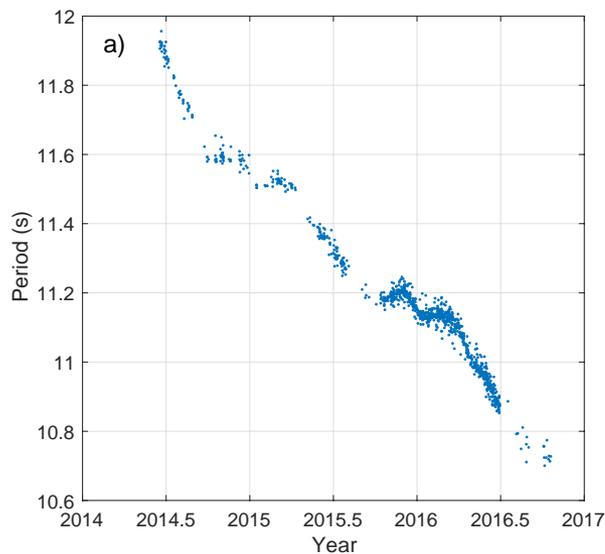


- Application of D-SPOSE to TOPEX/Poseidon in order to shed light on spacecraft rotational dynamics
- Possibility to investigate its unknown spacecraft parameters (moments of inertia, magnetic properties, etc...)

SLR Observations



- High repetition rate SLR observations show **increase in spin period** due to solar radiation pressure (Kucharski et al., 2017)
- **Oscillations in spin axis** elevation and azimuth are present
- Can D-SPOSE replicate these observations?
- Most important parameters, moments of inertia, are unknown



Moments of Inertia from Observations



- Gravity-gradient torque forces closed loop motion in reference frame precessing with the orbit (Holland and Sperling, 1969).
- From observation of spin axis (z-axis), we can obtain relationship between moments of inertia as a function of orbital parameters and spin axis orientation:

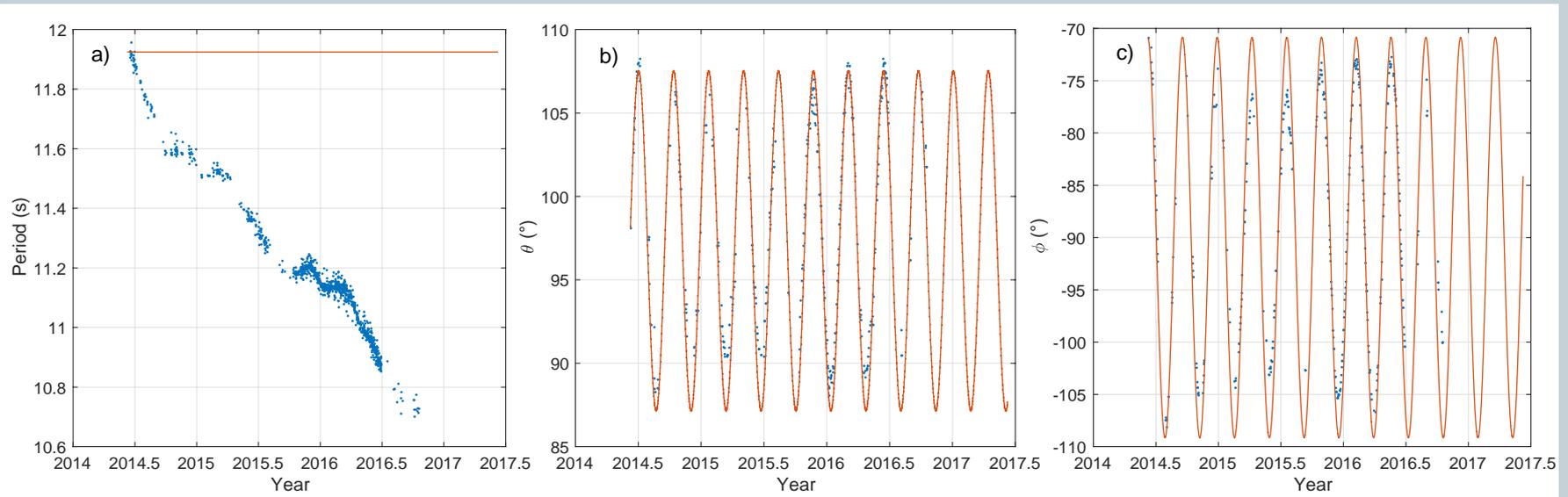
$$\frac{d\mathbf{L}}{dt} = \frac{3m}{4r^3} \frac{H}{L^2} L_z \begin{bmatrix} -L_y \\ L_x \\ 0 \end{bmatrix} - \boldsymbol{\omega} \times \mathbf{L} \quad \text{and} \quad \frac{I_x + I_y - 2I_z}{I_z} = \frac{4r^3 \omega}{3\mu} (-\dot{\Omega} \sin i \csc \theta \sin \phi + \dot{\Omega} \cos i \sec \theta)$$

- From SLR observations, it was found that: $I_x + I_y = 2.83I_z$
- Spacecraft in a stable minor-axis spin?

Gravity-Gradient Torque Only



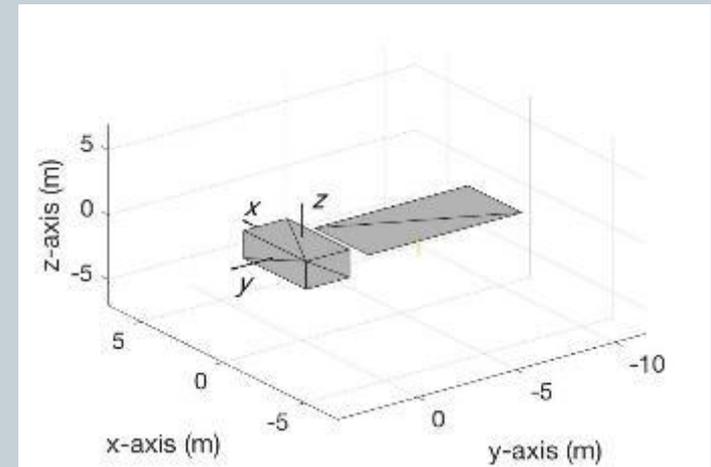
- Using $I_x + I_y = 2.83I_z$
- Results independent of I_x , I_y , and I_z as long as relationship holds



Propagator Input



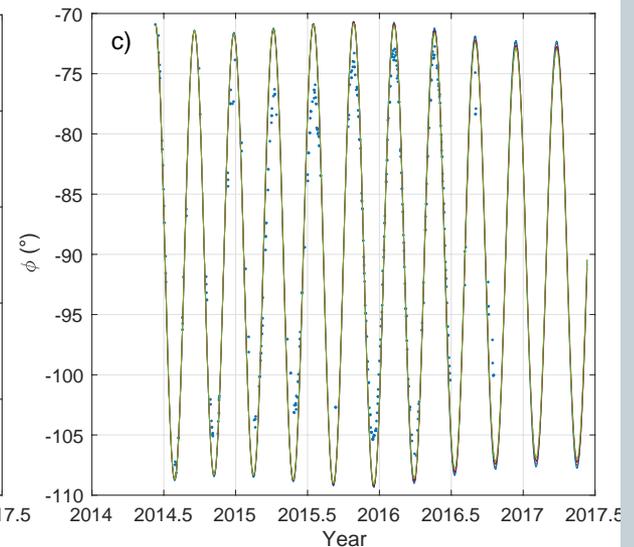
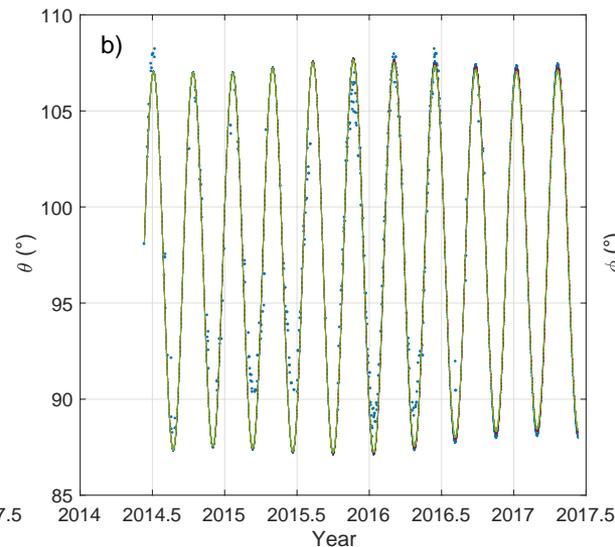
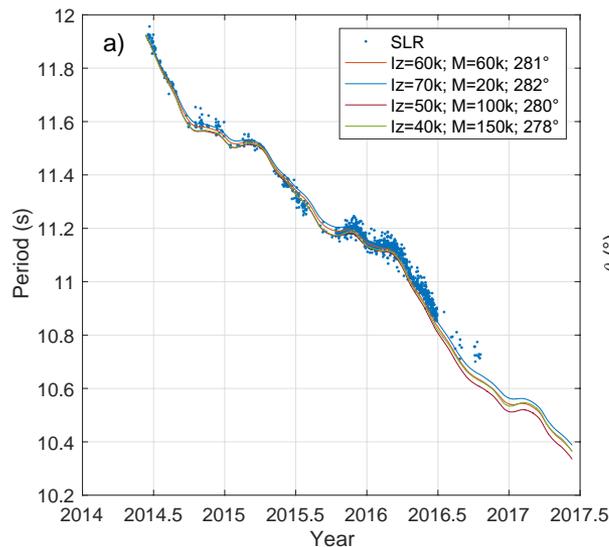
- Other unknowns include the **magnetic properties** (eddy-current torque) and **the spacecraft geometry** (orientation of solar panel plays large role in effect of SRP)
- Spacecraft spinning counterclockwise about z-axis
- I_z was varied from 70k to 40k kg m²
- Axisymmetry assumed ($I_x=I_y$); further tested afterwards
- Magnetic tensor and solar panel orientation (rotating about y-axis) were varied to fit observations



Simulation Results



- Spin evolution **well captured** by various simulations
- Amplitude of oscillations were found to vary due to radiation pressure
- Approx. **linear relationship between I_z and M** : $I_z = 75000 - 0.25M$
- Solar panel orientation close to Kucharksi et al. (2017) value
- Even with Kane damper, **spacecraft in stable minor-axis spin** (depending on damper characteristic: when dissipation is strongest, spacecraft eventually evolves into major-axis spin after a few years)



Conclusions



- From observations, a relationship between the moments of inertia was determined: $I_x + I_y = 2.83I_z$
- A linear relationship exists between I_z and M : $I_z = 75000 - 0.25M$; relationship between I_x and I_y is unknown.
- Simulations show TOPEX/Poseidon is spinning in a stable manner about minor axis
 - Currently doing energy checks to validate this
 - Looking at effect of Kane damper characteristics on spin stability
- A maximum value of I_z is 75,000 kg m²; obtaining a better estimate of the magnetic tensor will provide additional info on the moments of inertia, which, in turn, will provide more accurate estimate of solar panel orientation
- D-SPOSE will be **publicly available** by end of 2018 / early 2019 on the McGill Aerospace Mechatronics Laboratory GitHub: <<https://github.com/McGill-AML>>