



# **Investigation and Compensation of Detector Time Delays caused by Receive Signal Intensity Fluctuations**

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## **Accuracy of a measurement:**

### Single Shot Precision:

Uncertainty of the measurement, increased repetition rate leads to high Normal Point Precision

### Trueness (range bias):

Deviation of the measurement to the „real“ value, e. g. asymmetric return signal distribution leads to biases

## **Error sources in SLR:**

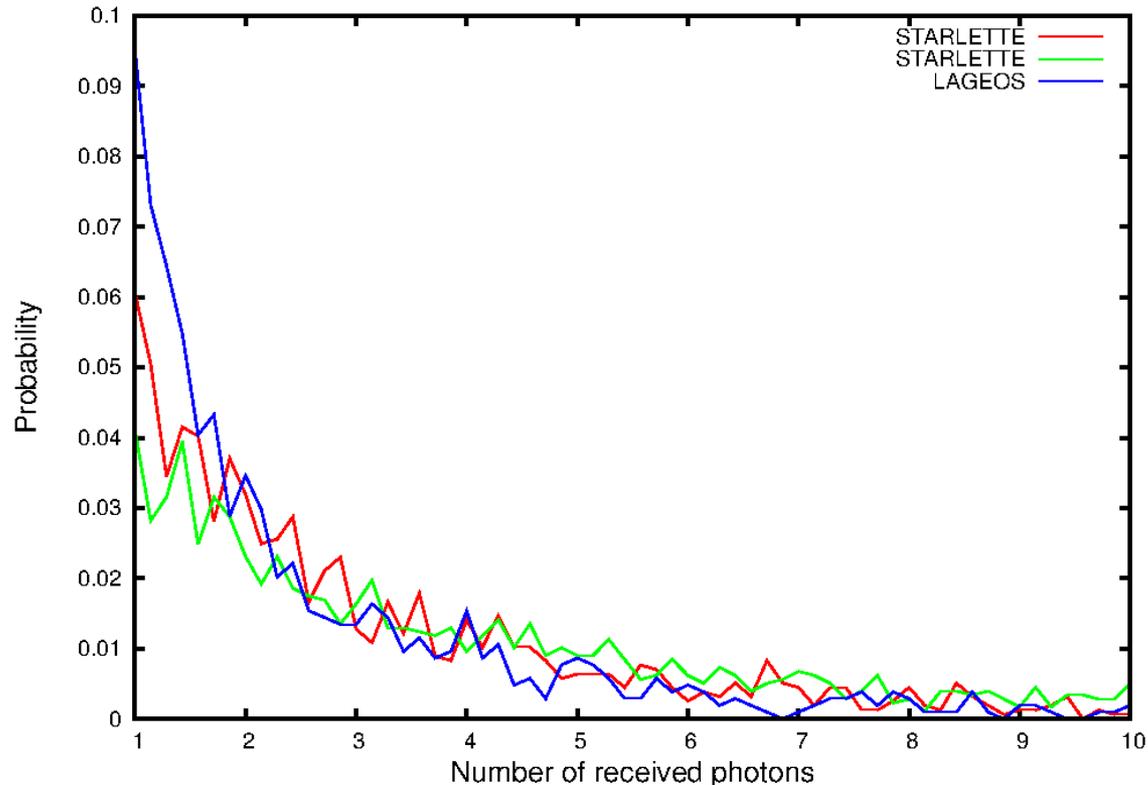
- Atmospheric contribution
- Satellite Signature
- Laser stability and pulse length
- **Intensity dependent detector time delays, ...**



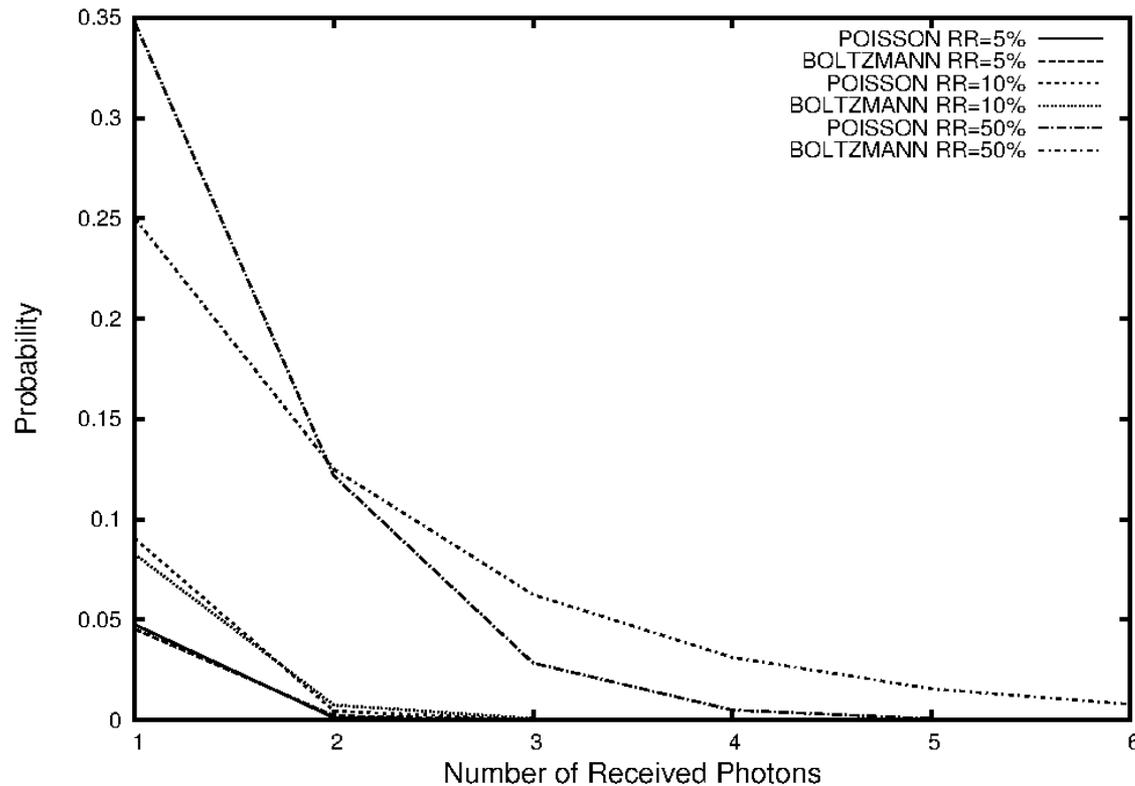
# Intensity Fluctuations - Experimental Characterisation-

Investigation of quantity and distribution of intensity fluctuations by means of a linear photodetector (MCP)

→ Return Signal Intensity is Boltzmann-distributed



Laboratory: During the calibration of an SLR-System the signal is Poisson-distributed (ideal Laser)  
=> Similar return rate may lead to different mean signal level





# Intensity Fluctuations - Summary & Problems -

Good: return rate  $< 10\%$   
=> intensity distributions comparable even for small variations, however: no single photons

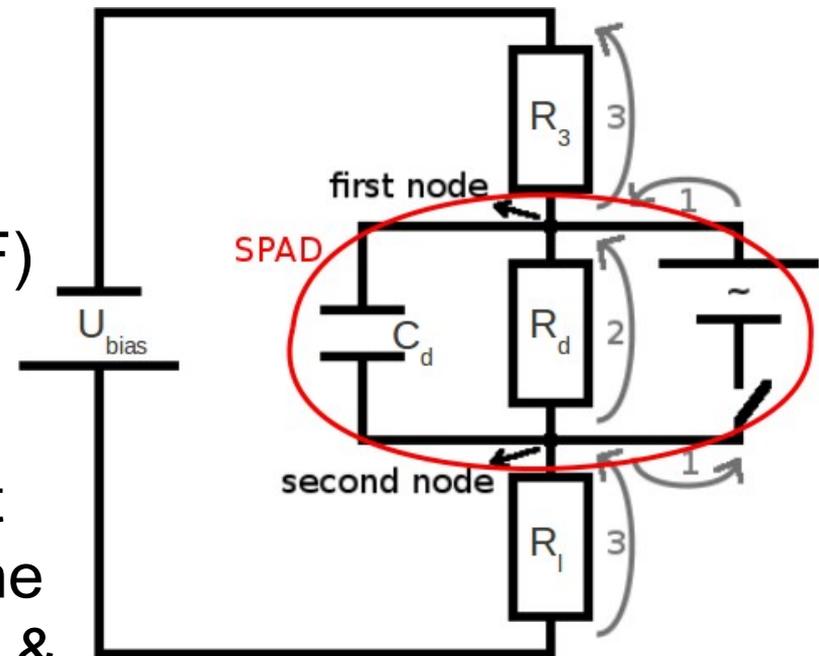
Problems: How to ensure a true Return Rate  $< 10\%$ , consider e. g.: daylight noise, dark noise, small clouds, plane trails, telescope pointing  
- In our measurements both did never match! -

Approach: Find a dependency of the intensity dependent detection delays on the output pulse-shape (peak-voltage, rise-time) for an InGaAs/InP-SPAD @ 1064nm and compensate the intensity dependent delays via postprocessing

# Intensity Dependent Delays - electrical circuit -

Add resistor ( $R_3$ ) to bias circuit:

- => Diodes Anode decoupled from current source
- => Capacity of SPAD (few pF) drives avalanche breakthrough
- => Small variations in current through ionized parts of the diode reduce bias voltage & gain (the longer an avalanche lasts [Timewalk], the wider it spreads laterally on the chip)

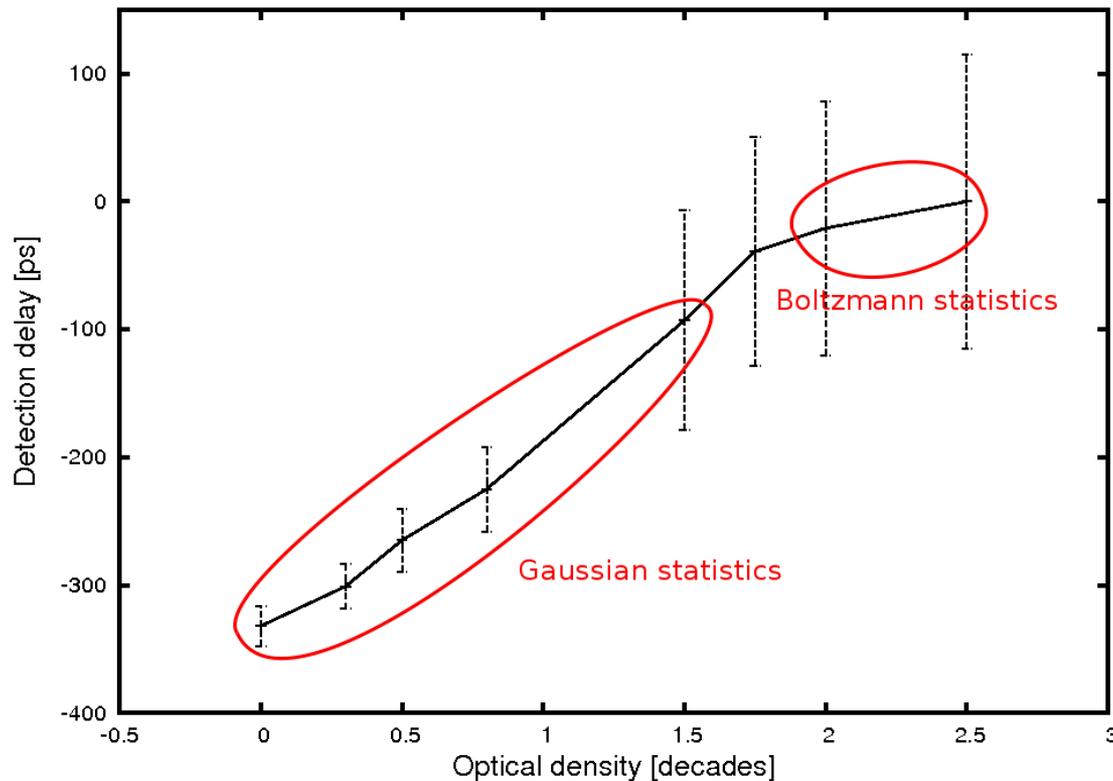


# Intensity dependent delays - Quantity -

Measure a constant distance (Calibration)

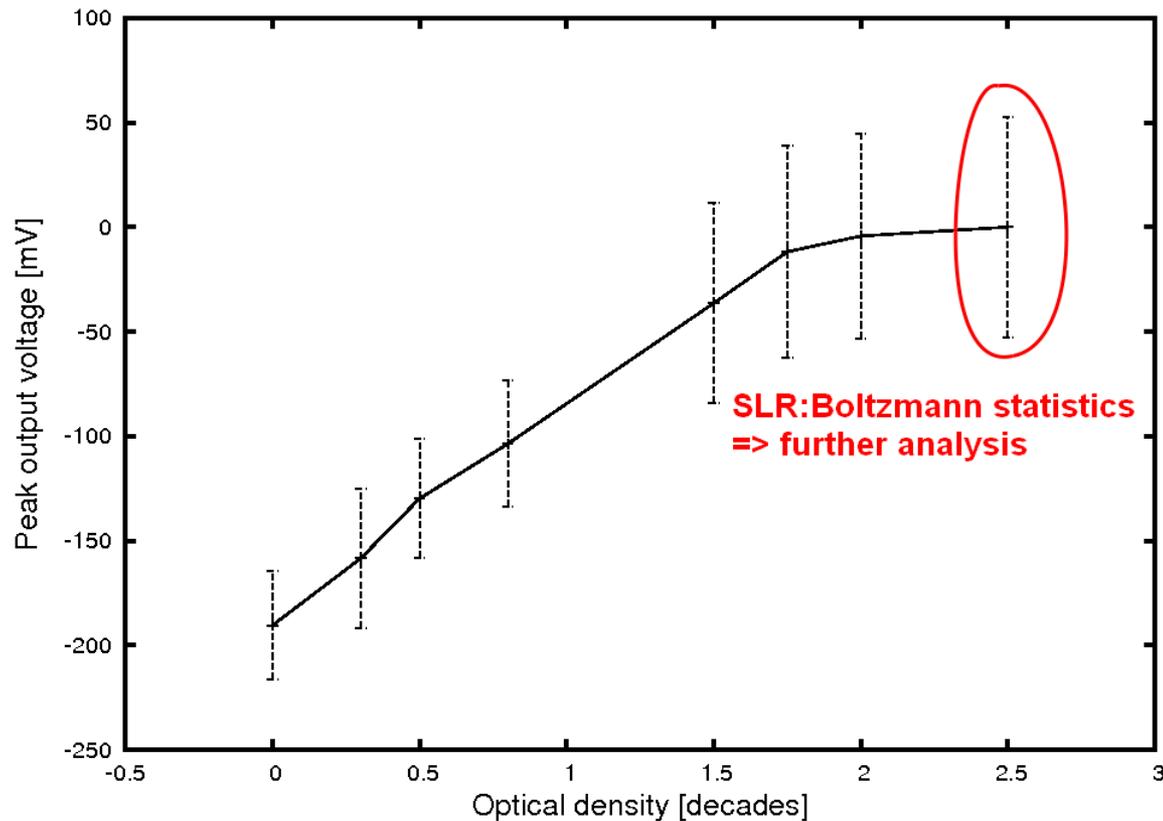
Simulate Boltzmann distribution (Multi Mode Fibre)

Use neutral density filters to adjust signal level



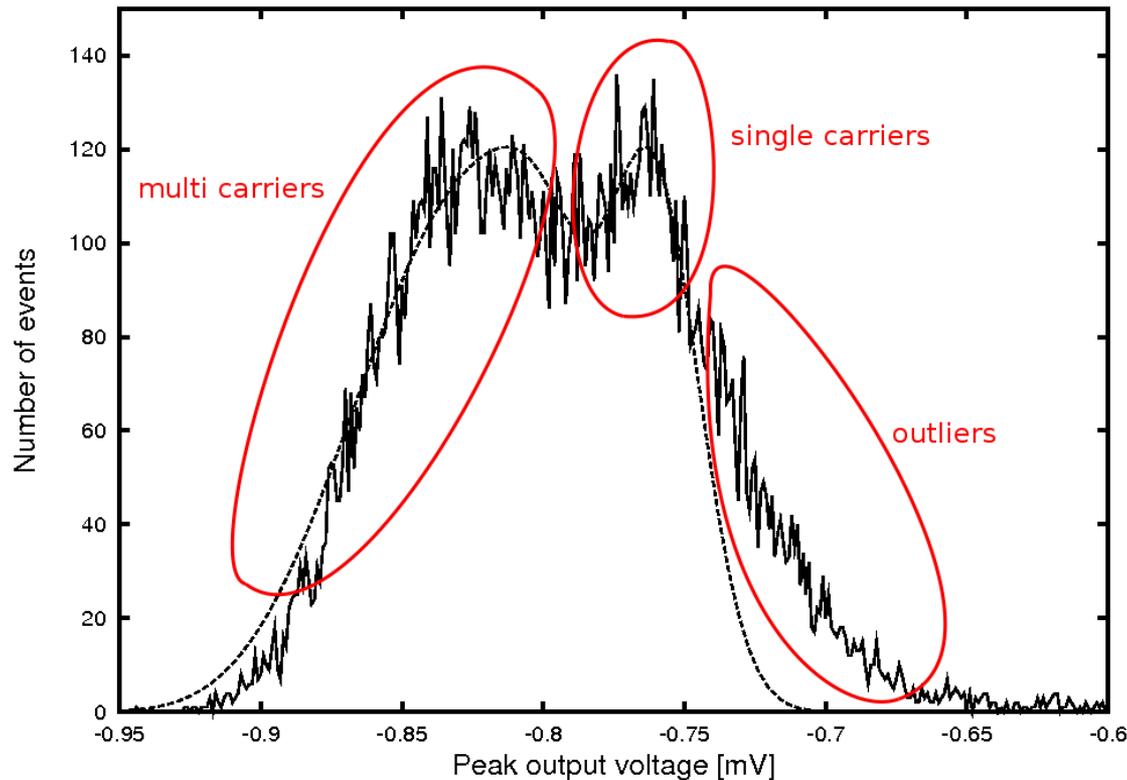
# Intensity dependent delays - Dependencies -

Simultaneously the peak output voltage was measured  
Same characteristics



# Intensity Dependent Delays - Peak Distribution -

- Peak distribution: - distinct single carrier multiplication peak  
(@21% count rate) - broad multi carrier multiplication peak
- Reason: logarithmic dependence → modelling



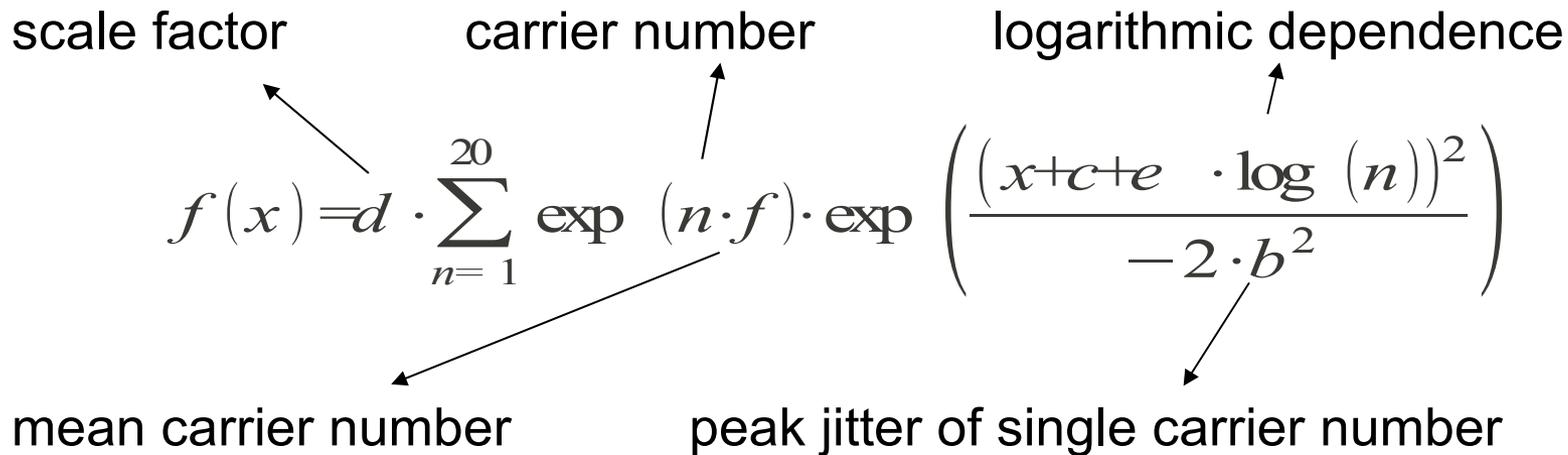
# Intensity Dependent Delays - Modelling -

- 20 Gaussian distributed functions, each representing a specific carrier number
- Boltzmann statistics (multi mode fiber at low light level)

scale factor                      carrier number                      logarithmic dependence

$$f(x) = d \cdot \sum_{n=1}^{20} \exp(n \cdot f) \cdot \exp\left(\frac{(x+c+e \cdot \log(n))^2}{-2 \cdot b^2}\right)$$

mean carrier number                      peak jitter of single carrier number





Intension: Find mean carrier number to get probabilities of each carrier number & compensate intensity dependent delays based on these probabilities

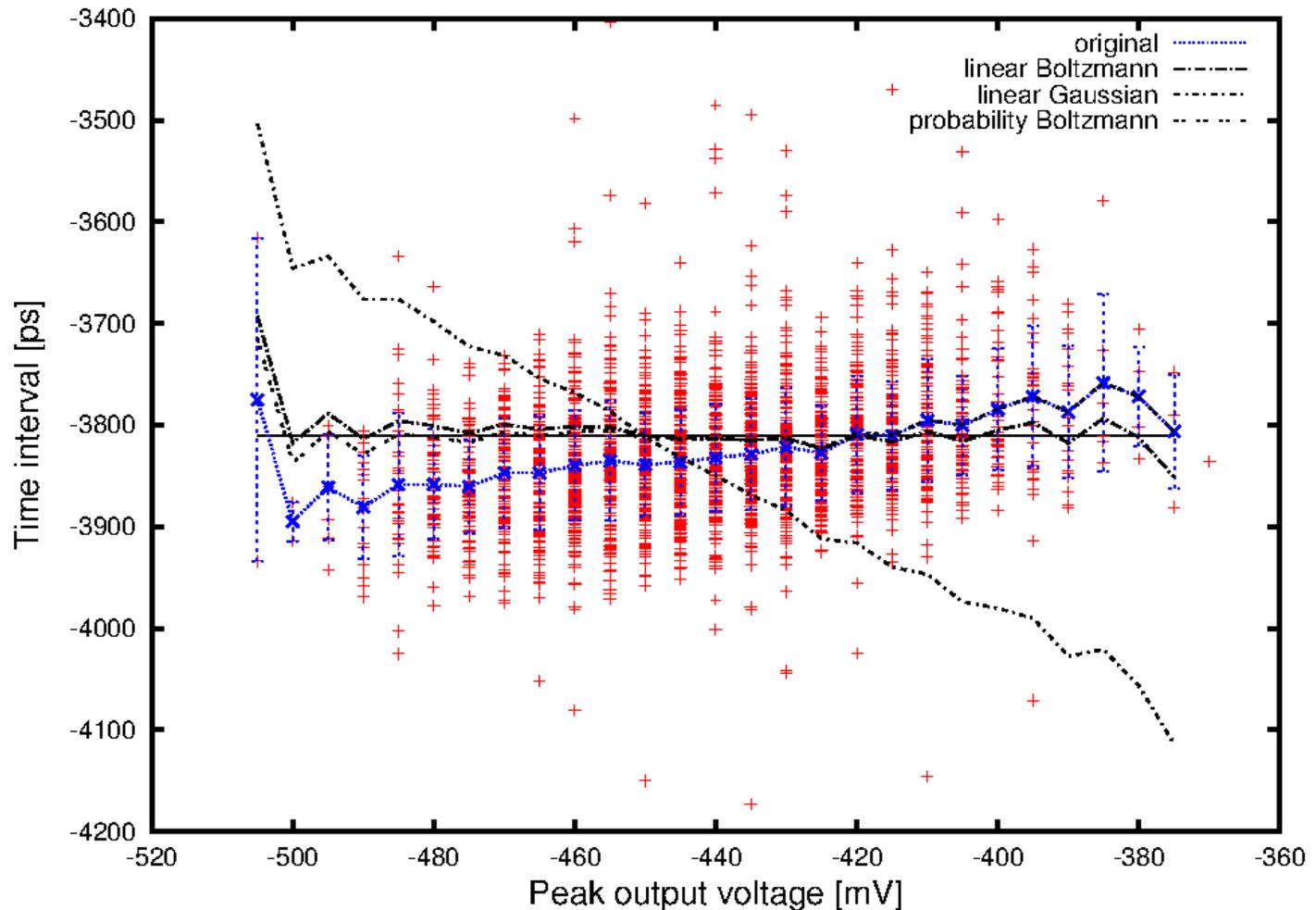
Investigation of three compensation strategies by recording each single event:

- 1) linear approach based on symmetric Gauß-Statistics (Slope at high light intensities)
- 2) linear approach based on fitting the distribution (not possible during SLR measurement, no fixed distance)
- 3) approach based on the mean photon number (derived from modelling with Boltzmann-statistics)



# Compensation - Results Strategies -

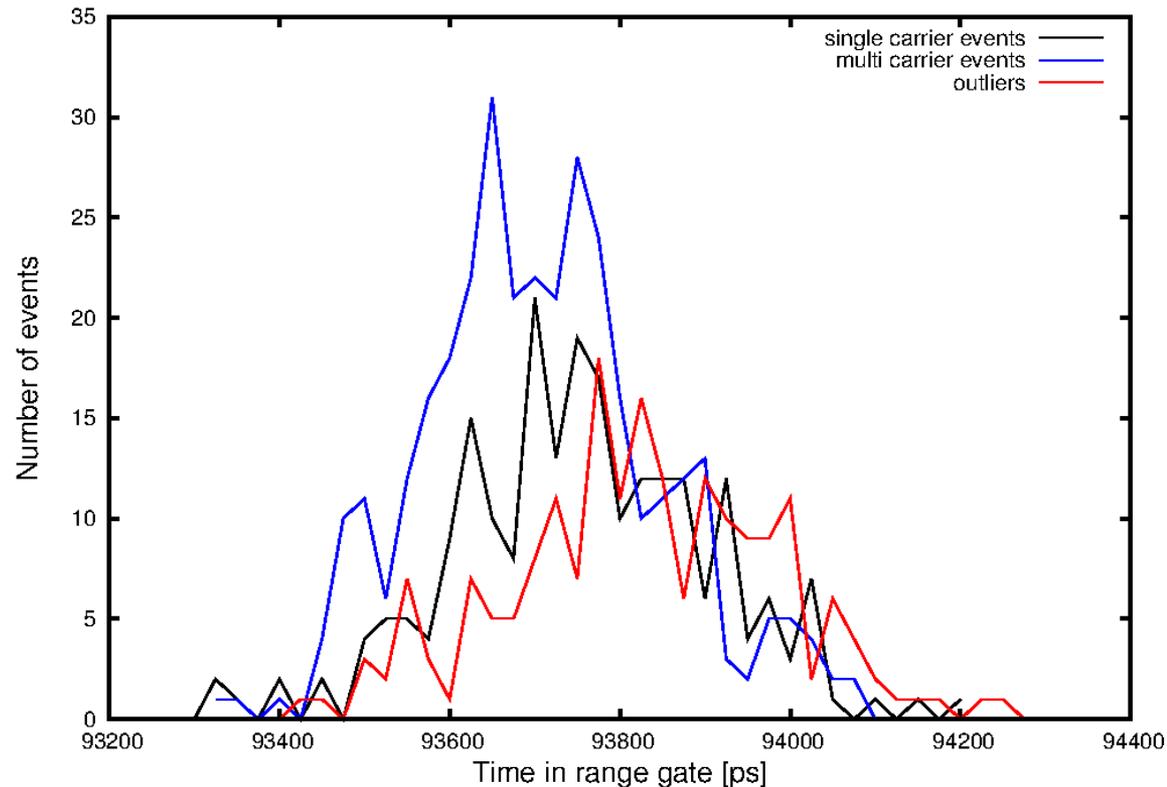
Ideal: get a constant time interval for any peak voltage





# Compensation - Return Signal Distribution -

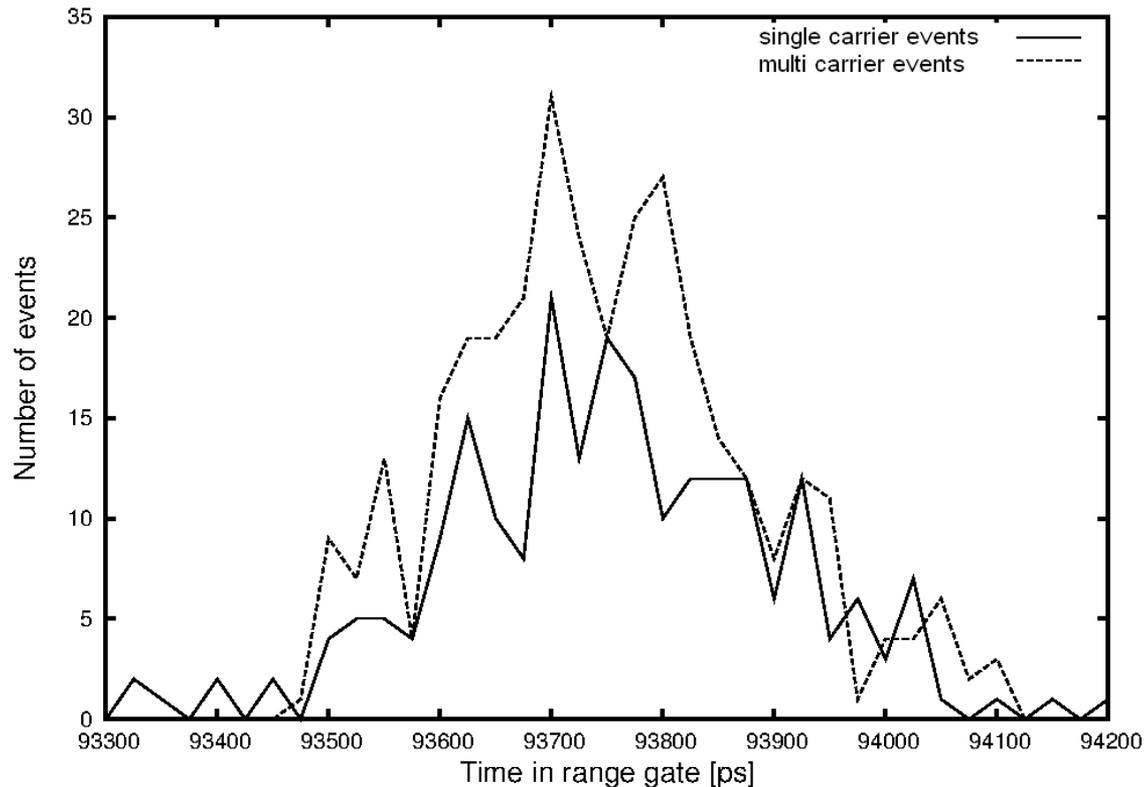
- Distributions of the return signal in range gate for different regions of the peak voltage
- Shift in mean value for single and multi-carrier signals, outliers in peak voltage are also outliers in the ToF measurement





# Compensation - Compensated Distribution -

- Compensation approach matches the distributions
- Satellite signature of GLONASS visible to some extent





- The return signal distribution seems to follow Boltzmann-Statistics for a high dynamic range
- An approach was developed to find the mean return signal level
- This information was successfully used for compensation of intensity dependent detection delays
  
- Physics for silicon is the same => apply to Si SPADs
- Still pending: Orbit determination based on the results
- Maybe: analysis of satellite signature for single/multi photon returns